

Recap:- ① Haldane model

↳ on a unit cell it doesn't break TRS

↳ but overall it does break TRS

② TRS → cons broken by phase term

↳ sign of phase oscillates

$$H = t_1 \sum_{\langle ij \rangle} c_i^\dagger c_j + t_2 \sum_{\langle\langle ij \rangle\rangle} e^{-i D_{ij} \phi} c_i^\dagger c_j + M \sum_i c_i^\dagger c_i$$

$$D_{ij} = \text{sign} \begin{pmatrix} \hat{d}_1 \\ \hat{d}_2 \end{pmatrix}$$

Note: these vectors are parallel but the phase they will pickup

Nearest + 1st neighbor

$$t_2 \leq c_i^\dagger c_j e^{-i D_{ij}(\phi)}$$

$\langle\langle ij \rangle\rangle$

→ spin isn't taken into account

→ 2x2 hamiltonian effective low energy hamiltonian

⇒ Gap opening & closing → as you vary phase term

↙ leads to boundary modes!

In general

$$H(\mathbf{r}) = R_a A_{ab} \sigma_b + M \sigma_3$$

Then

$$\sigma_{\text{avg}} = \frac{1}{2} \text{Sign}(M) \text{Sign}(\text{Det} A)$$

I have derived this using

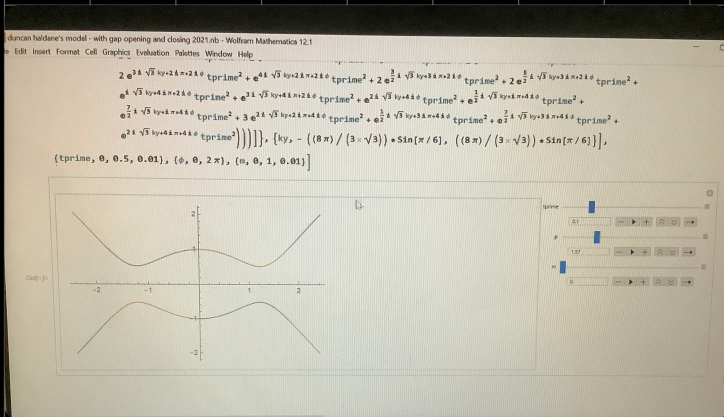
finite ribbon implementation [what is the reason for Bulk-boundary correspondence?]

why isn't there a phase on m ?
 ↳ net flux over

+1 • +1
 • -1

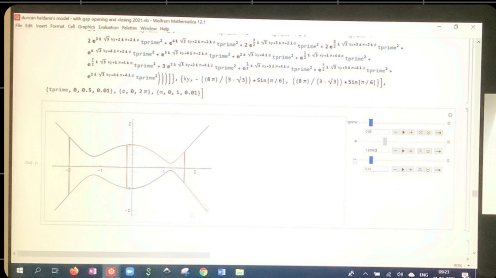
Haldane → think of ϕ_{Hall} as a chern insulator
 ↳ break TRS without adding B^0 explicitly

Do HW problems



high symmetry points

phase term → lifts symmetry b/c two valleys



phase → closes gap

site A/site B twisting of the axes

trivial → some sites weight weight

non- " → size changes

Play with mathematica

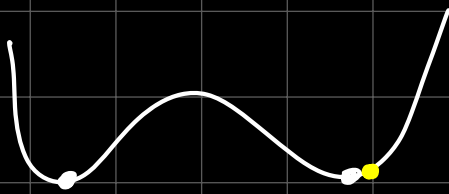
↳ "twisting" of bonds

↳ gap closing in k-space

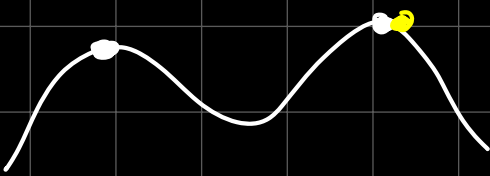
Gap closing in real space

@ Vanderbilt's
Book

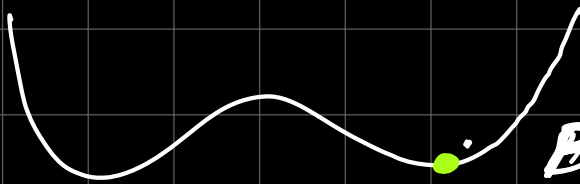
Python
Package



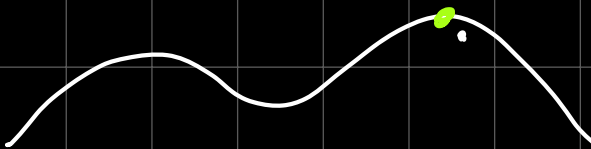
• → Alike
• → Blike.



after
gap closing

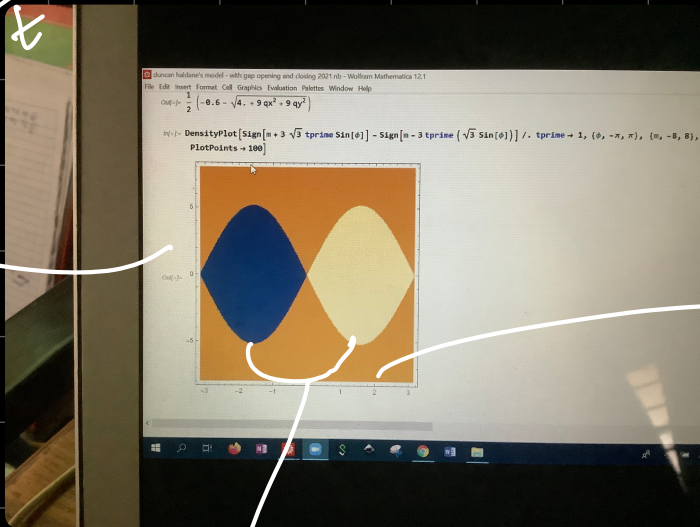


Blike character



* Chern # → sum over 2 valleys → not zero chern #
which change
sign

ratio of $\frac{\pi}{2}$

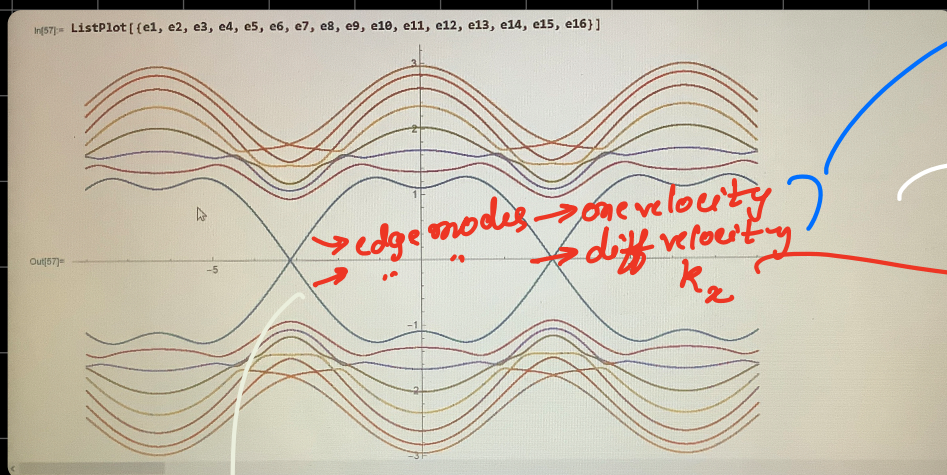


phase

$$\psi = \frac{-\pi}{2} \text{ to } \frac{\pi}{2}$$

Ribbon realizatⁿ of same mode!

↳ painful book keeping but simple calculation



→ one circulates in 1 direction & other in other direction

↳ gaps spectrum

→ along the length of ribbon

* we have a circulating current itself

Chern # $\Rightarrow$ magnetizatⁿ of the system

Q Hall $\rightarrow$ eqn no current?
↳ dumb law

↳ live on one side
↳ live on other side

